

# Design and FPGA implementation of 11<sup>th</sup> order Efficient IIR Wavelet Filter Banks with Approximate Linear-phase

Rasha Waleed Hamad  
College of Engineering, University of Mosul, Mosul, Iraq

## ABSTRACT

In this paper. Bireciprocal Lattice Wave Digital Filters (BLWDFs) are utilized in an approximate linear-phase in pass-band design of 11<sup>th</sup> order IIR wavelet filter banks (FBs). These filter banks are efficiently designed by replacement one of branches for (BLWDFs) by only a unit delay. The coefficients of the designed filter are achieved by simulating the IIR response suggested in [1]. The design is first simulated using Matlab programming in order to investigate the resulting wavelet filter properties and to find the suitable wordlength for the BLWDFs coefficients. FPGA implementation of the proposed IIR wavelet filter bank is also achieved for three levels with less complexity and high operating frequency.

**KEYWORDS :** Bireciprocal Lattice Wave Digital Filter(BLWDF), All-pass sections, IIR Wavelet Filter Banks, Approximate Linear-phase, FPGA implementation.

## 1. INTRODUCTION

Two-channel perfect reconstruction (PR) filter banks have been used in different applications of signal processing, such as subband coding of speech and image signals, transmultiplexers, and voice privacy systems [2]. Filter banks can be realized using finite impulse response (FIR) or infinite impulse response (IIR) filters [3]. Perfect Reconstruction (PR) IIR filter banks are very attractive because of their potentially low system delay and better frequency responses compared with their FIR FBs [4]. H. W. Löllmann and P. Vary [5] in 2008 proposed a new design for a two-channel IIR QMF bank with near-perfect reconstruction (NPR). The analysis filter bank is given by an efficient polyphase network (PPN) implementation based on all-pass filters. These filter banks have a significantly lower algorithmic complexity and causes no or negligible amplitude distortions. This design can be beneficial for coding and transmission applications. In 2009 R. Ramanathan and K. P. Soman [6] presented a novel technique for designing an IIR filter with linear-phase response. This technique uses the frequency domain sampling along with the linear programming concept to achieve a filter design, which gives a best

approximation for the linear phase response. The proposed method can give the closest response with less number of samples (only 10) and is computationally simple. Filter design is presented along with its formulation and solving methodology. Numerical results are used to substantiate the efficiency of the proposed method. In 2011 Jassim. M. A. and Rasha. W. H. [7] designed 9<sup>th</sup> order IIR wavelet filter banks utilizing Bireciprocal Lattice wave Digital Filters (BLWDFs) with approximate linear phase. Each of the two branches in the structure of the BLWDF realizes an allpass filter. Filter coefficients has been quantized then realized in a multiplierless manner taking into account the low-coefficient sensitivity property of these wave structures. FPGA implementation of such IIR wavelet filter is achieved with less complexity. In 2012, Jassim. M. A. and Sama. N. M. [8] designed a new filter bank structure, for the implementation of discrete wavelet transform. Such structure is based on the idea of the Bireciprocal Lattice Wave Digital Filters (BLWDFs) to simulate the two channel wavelet filter bank for six levels. Linear-phase reconstruction is not treated in such structure. In this paper, 11<sup>th</sup> order IIR wavelet filter banks are efficiently designed and implemented with perfect reconstruction and approximate linear-phase properties by utilizing bireciprocal lattice wave filter (BLWDF) with the replacement one of its channels by a pure delay unit. The proposed design is then implemented on Spartan-3E FPGA kit. For fast hardware implementation on an FPGA, the filter coefficients are implemented in a multiplierless manner after representing them as sum-and-difference-of-

powers-of-two (SPT). All multiplications are then achieved by shift and add.

**2. THE PROPOSED Design**

The design of approximately linear phase IIR wavelet filter has been obtained by letting one of the branches

$z^{-1}A_1(z^2)$  in the BLWDF be a pure delay ( $z^{-(2R+1)}$ ) as shown in Fig. 1. The other branch  $A_0(z^2)$  (of even order  $2N$ ) is a general all-pass function in  $z^2$ , which can be realized by cascading all-pass sections [9].

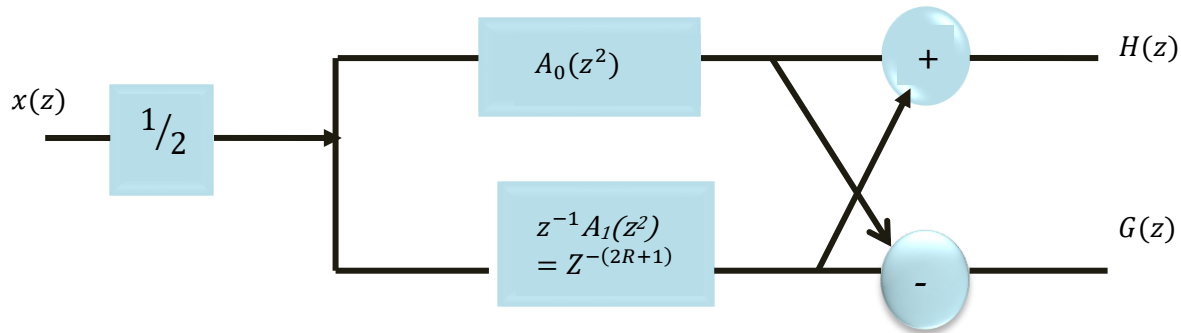


Fig (1) : Approximate linear-phase BLWDF

The transfer function of an approximate linear-phase low-pass BLWDF is

$$H(z) = \frac{1}{2} [A_0(Z^2) + Z^{-(2R+1)}] \tag{1}$$

where R is the number of attenuation zeros. For the design of a 11th order IIR wavelet filter of this type, we chose N= 3 and R=2, then  $A_0(z^2)$  can be written as

$$A_0(z^2) = \frac{z^{-6}+az^{-4}+bz^{-2}+c}{cz^{-6}+bz^{-4}+az^{-2}+1} \tag{2}$$

and

$$H(z) = \frac{1}{2} \left[ \frac{z^{-6}+az^{-4}+bz^{-2}+c}{cz^{-6}+bz^{-4}+az^{-2}+1} + Z^{-5} \right] \tag{3}$$

Equation (3) can be written as

$$H(z) = \frac{1}{2} \left[ \frac{c+bz^{-2}+az^{-4}+z^{-5}+z^{-6}+az^{-7}+bz^{-9}+cz^{-11}}{cz^{-6}+bz^{-4}+az^{-2}+1} \right] \tag{4}$$

Also, substituting  $z^{-1} = e^{-j\omega}$  in (4), results

$$H(e^{j\omega}) = \frac{1}{2} \left[ \frac{c+be^{-j2\omega}+ae^{-j4\omega} + e^{-j5\omega}+e^{-j6\omega}+ae^{-j7\omega}+be^{-j9\omega}+c e^{-j11\omega}}{ce^{-j6\omega}+be^{-j4\omega}+ae^{-j2\omega}+1} \right] \tag{5}$$

The coefficients a,b and c are determined by compared the magnitude response for the designed filter with desired magnitude response for 11<sup>th</sup> order intermediate filter which is given in [1]. The values of a, b and c

which give minimum error between the two designs (0.0051) are a=0.5 , b=0.25 and c=-0.05. The magnitude responses for two designs are shown in Fig. 2.

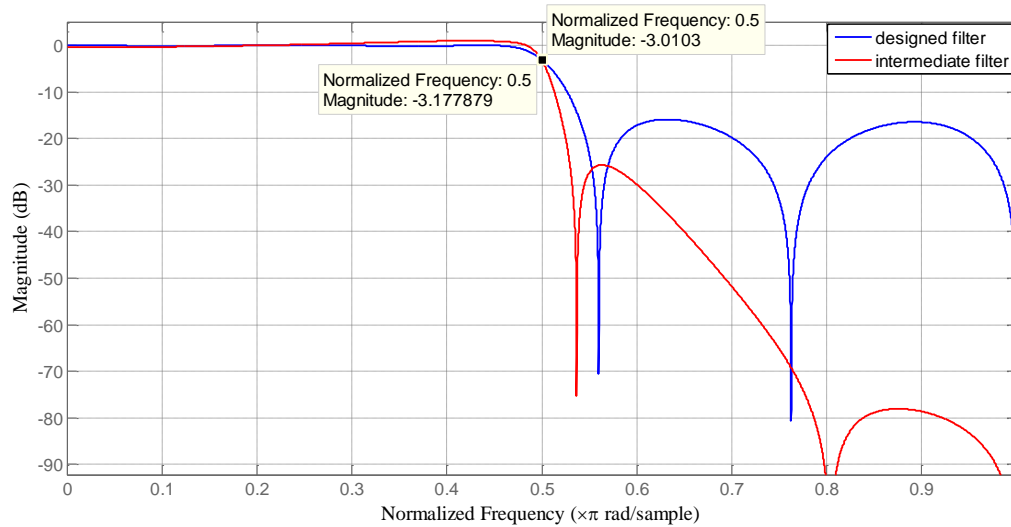


Fig (2) : Magnitude responses of designed filter and desired intermediate filter in [1]

Substituting these coefficients in (4) resulting *IIR* 11<sup>th</sup> order *BLWDF* low-pass transfer function

$$H(z) = \frac{1}{2} \left[ \frac{-0.05 + 0.25z^{-2} + 0.5z^{-4} + z^{-5} + z^{-6} + 0.5z^{-7} + 0.25z^{-9} - 0.05z^{-11}}{-0.05z^{-6} + 0.25z^{-4} + 0.5z^{-2} + 1} \right] \quad (6)$$

The frequency response for the designed filter is shown in Fig. 3.

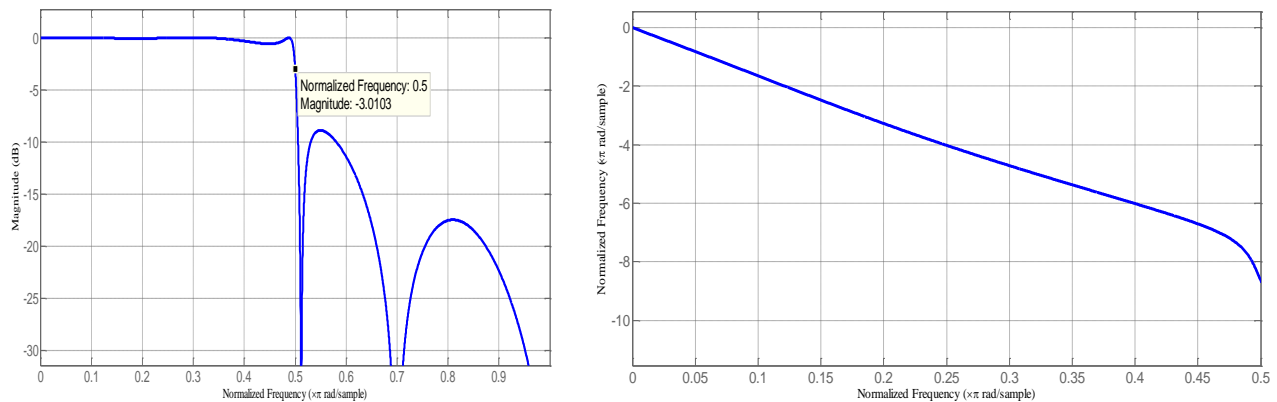


Fig (3) : Frequency response of 11<sup>th</sup> order *IIR* wavelet filter

From Fig. 3, it can be seen that the phase response of the designed filter is almost linear. Linear-phase response can be measured by “deviation from linear phase”. It is defined as a Distance of each point of a phase response

of designed filter from the phase response of ideal filter [10]. Fig.4 shows the phase deviation from linear phase of designed filter.

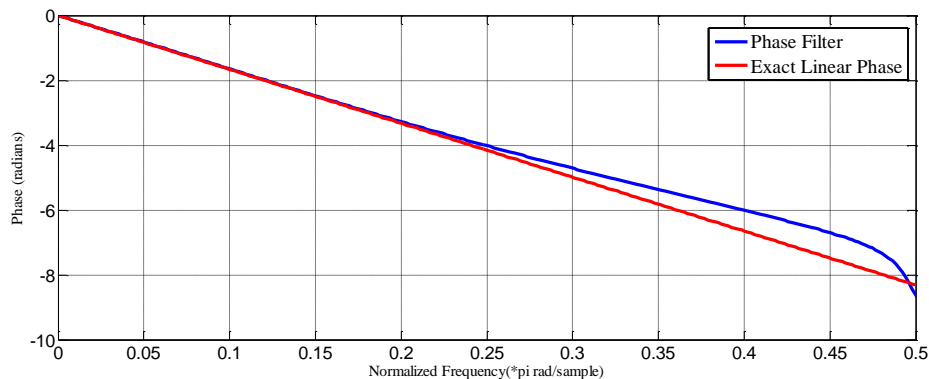


Fig (4) : The phase deviation from linear-phase of the designed filter

for stable and efficient realization, the structure in Fig. 5. is used with is  $A_0(z)$  rewritten in the following equation [11][12] :

$$A_0(z) = \frac{z^{-3} + az^{-2} + bz^{-1} + c}{cz^{-3} + bz^{-2} + az^{-1} + 1} \quad (7)$$

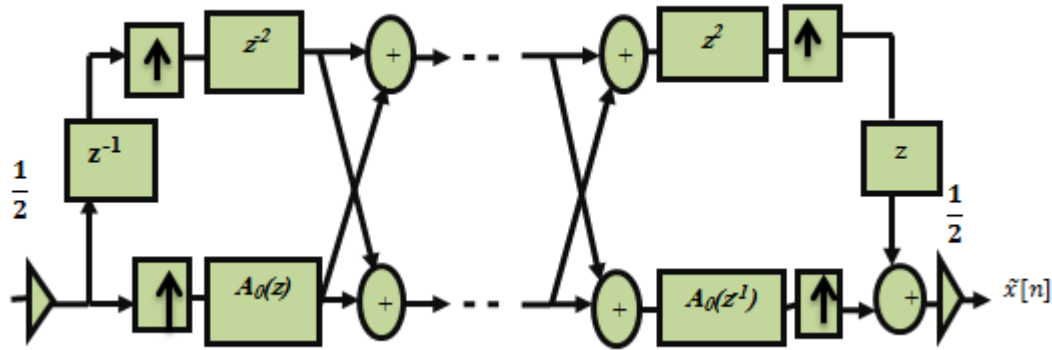


Fig (5) : An efficient structure for IIR wavelet filter bank

The all-pass function  $A_0(z)$  can be expressed in a product form as in 8

$$A_0(z) = \frac{\alpha + z^{-1}}{1 + \alpha z^{-1}} * \frac{\beta + z^{-1}}{1 + \beta z^{-1}} * \frac{\gamma + z^{-1}}{1 + \gamma z^{-1}} \quad (8)$$

where the values of  $\alpha$  ,  $\beta$  and  $\gamma$  are 0.745400849956, 0.16388878629124 and -0.40928965880625, respectively.

The resulting mother wavelet and scaling functions for designed filter shown in Fig. 6, can be generated after

five iterations of the analysis filter banks on its low-pass branch.

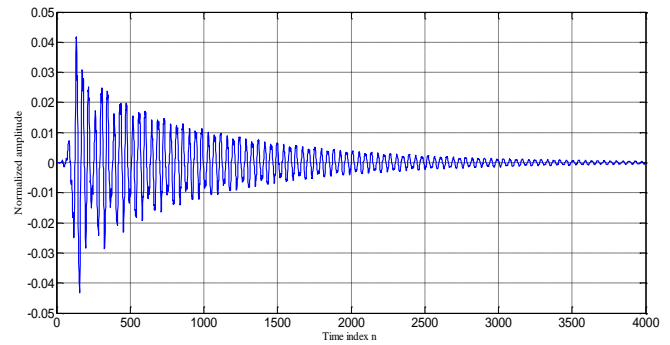
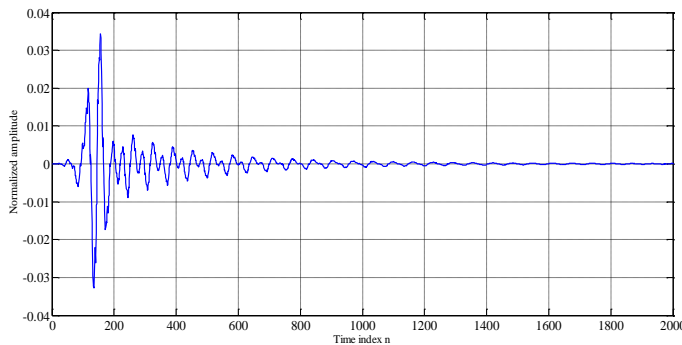


Fig (6) : The wavelet function and scaling function for the proposed design: (a) wavelet function (b) scaling function

### 3.OBJECTIVE AND SUBJECTIVE QUALITY METRICS

Different quality metrics exist in practice to evaluate the quality of the signal processing algorithms. Quality measures may be very subjective when based on human perception or can be objectively defined using mathematical or statistical evaluations. the most widely used objective quality metricses are the Signal-to-Noise Ratio (SNR), Peak Signal-to-Noise Ratio (PSNR) and Correlation factor (Cor)[13][14].

### 4. MATLAB SIMULATION RESULTS

The proposed designed filter bank is described using

Matlab programming for verification and selection a sufficient wordlength, Some Gray scale images (as shown in Fig. 7) are used to find the minimum wordlength of the BLWDFs coefficients for acceptable PSNR and SNR values which are considered to be about 30dB. The correlation coefficient has a close to one-value. The best selected 6-bit wordlength is chosen, which gives the values of the objective quality metricses illustrated in Table (1). These measures show an excellent closeness to the ideal case. Thus BLWDF coefficients after quantization are  $\alpha=0.75, \beta =0.15625$  and  $\gamma = -0.40625$ .



Fig (7) : The results of Matlab simulation for the 11<sup>th</sup> order IIR wavelet filter bank on Lena and Barbara images

TABLE (1) : The objective quality metrics of the proposed design after quantization

	Lena	barbara
PSNR (dB)	51.2664	41.2501
SNR (dB)	41.8422	35.3071
Correlation	0.9998	0.9991

**5. FPGA IMPLEMENTATION**

The proposed design is described with VHDL language. Then an FPGA device is used to implement the filter design. It is a 500,000-gate Xilinx Spartan-3E XC3S500E in a 320- ball Fine-Pitch Ball Grid Array package (XC3S500EFG320). FPGA implementation is presented for one level and multi-levels. Multi-levels implementation is achieved using bit-serial technique which is usually used to reduce implementation cost

because of that the hardware resources needed for it are very modest [15]. Bit-serial implementation means constructing a structure that consists of similar cascaded processing elements by building only one of these processing elements and using it to perform the whole task. The implementation results for one level and three-levels are presented in tables 2.

TABLE (2) : The implementation results for one level and three-levels

	Analysis/ Synthesis	Resource	Used	Availa ble	Utiliz ation ratio
One- level	Analysis Side Structure	Slices	117	4656	2%
		Slice flip flops	108	9312	1%
		4-input LUTs	170	9312	1%
	Synthesis Side Structure	Slices	176	4656	3%
		Slice flip flops	163	9312	1%
		4-input LUTs	239	9312	2%

Multi-levels	Analysis Side Structure	Slices	353	4656	7%
		Slice flip flops	395	9312	4%
		4-input LUTs	480	9312	5%
	Synthesis Side Structure	Slices	375	4656	8%
		Slice flip flops	402	9312	4%
		4-input LUTs	463	9312	4%

## 6. CONCLUSIONS

In this paper, a 11<sup>th</sup> order IIR wavelet filter bank is efficiently designed and realized with approximate linear-phase in pass-band utilizing Bireciprocal Lattice Wave Digital Filters (BLWDFs). The values of the filter coefficients are quite suitable for implementation using shift and add operations instead of multipliers to perform multiplications. This is going to give very efficient hardware saving when implementing, in addition to the method of design with unit delay-all-pass replacement which also given efficiency in hardware area. The proposed design is first simulated using Matlab programming in order to investigate the resulting wavelet filter properties and to find the suitable wordlength for BLWDF's coefficients. FPGA implementations of one-level and multi-levels of bireciprocal lattice wave digital wavelet filter banks have been obtained with less complexity and high speed.

## REFERENCES

1. J. M. Abdul-Jabbar and Z. Z. Hameed (2013). " Design and Implementation of DWMT Transmission Systems using IIR Wavelet Filter Banks": Int. J. Com. Dig. Sys. 2, No. 3, pp. 159-167. Retrieved from <http://dx.doi.org/10.12785/ijcds/020307>.
2. Xi Zhang (1999). " Design of two-channel IIR linear phase PR filter banks ": Signal Processing 72, pp. 167-175.
3. S. Damjanović and L. Milić (2005). "Examples of orthonormal wavelet transform implemented with IIR filter pairs":The 2005 International 114 Workshop on Spectral Methods and Multirate Signal Processing- SMSP 2005, Riga, Latvia, pp. 19 - 27.
4. P.P.Vaidyanathan (1993). " Multirate Systems and Filter Banks": Englewood Cliffs, NJ: Prentice- Hall.
5. Heinrich W. L. and Peter V. (2008). "Design of IIR QMF Banks with Near-Perfect Reconstruction and Low complexity": Proceedings of IEEE International Conference on Acoustics, Speech, and Signal Processing (ICASSP), (Las Vegas, NV, USA), ISBN 978-1-42441-483-3, pp. 3521-3524.
6. H. W. L'ollmann and P. Vary (2009). "A Novel Methodology for Designing Linear- Phase IIR Filters": International Journal of Recent Trends in Engineering, Vol 1, No. 3.
7. J. M. Abdul-Jabbar and R. W. Hamad (2011). "Allpass-Based Design, Multiplierless Realization and Implementation of IIR Wavelet Filter Banks with Approximate Linear Phase": The Fourth IEEE International Symposium on Innovation in Information & Communication Technology (ISIICT 2011), Amman, Jordan, pp. 118 - 123.
8. J. M. Abdul-Jabbar and S. N. M. Al-Faydi (2012) "Design and Realization of Bireciprocal Lattice Wave Discrete Wavelet Filter Banks": Alrafidain Engineering Journal, Collage of Engineering, University of Mosul, Mosul, Iraq, Vol. 20, No. 1, pp. 38-48.
9. J. M. Abdul-Jabbar (2009) "An Analytical Design Procedure for Bireciprocal Lattice Wave Digital Filters with Approximate Linear-Phase": Alrafidain Engineering Journal, Collage of Engineering, University of Mosul, Mosul, Iraq, Vol. 17, No. 6, PP. 42-52.
10. Mini-Circuits, pub. "Band pass filters with linear-phase response": The Design Engineers Search Engine, REV. OR, M113292, AN-75-004, 070830, Page 1 of 3. On [www.minicircuits.com](http://www.minicircuits.com).
11. J. M. Abdul-Jabbar (1997) "Design procedures for two-dimensional digital filters and filter banks", Ph.D. Thesis, Department of Electrical Engineering, Basrah University, Iraq.
12. B. M. Lutovac and M. D. Lutovac (2002) "Design and VHDL description of multiplierless half-band IIR filter": International Journal Electronic Communication (AEU) 56, Faculty of Electrical Engineering, University of Montenegro, Yugoslavia, No. 5, pp. 1-3.
13. T. Acharya and P. Tsai (2005) "JPEG 2000 Standard for Image Compression": John Wiley & Sons, Inc., Hoboken, New Jersey, ISBN 0-07-252261-5.
14. H. H. Abdul zahrah (2004) "Encryption Using Wavelet coded Image Data": M.Sc. Thesis in Computer Engineering, Collage of Engineering, University of Basrah, Basrah, Iraq.
15. G. Hofferek (2008) "Exploring the Design Space of the GPS Authentication Scheme": Ms.c Thesis, Institute for Applied Information, Processing and Communications (IAIK), Graz University of Technology.